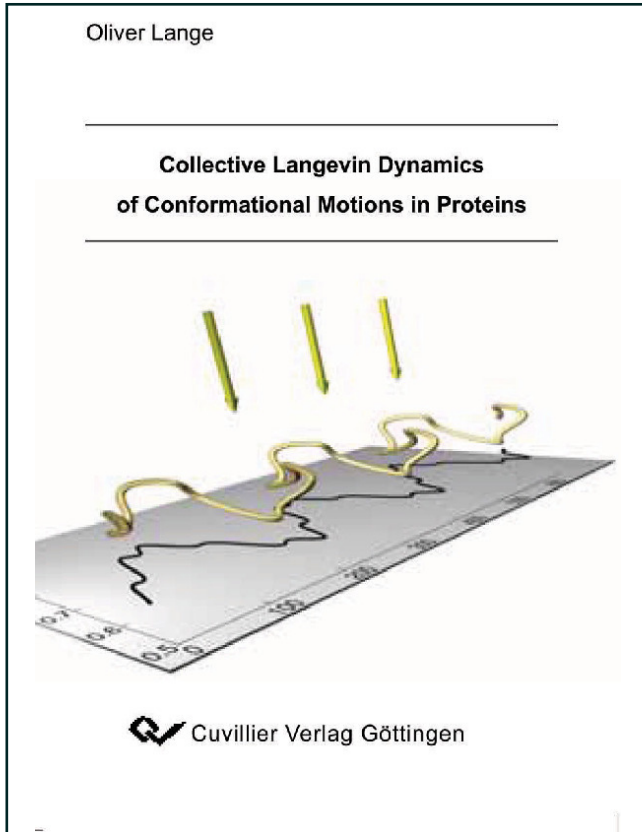




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**Collective Langevin Dynamics of Conformational Motions in Protein**



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